



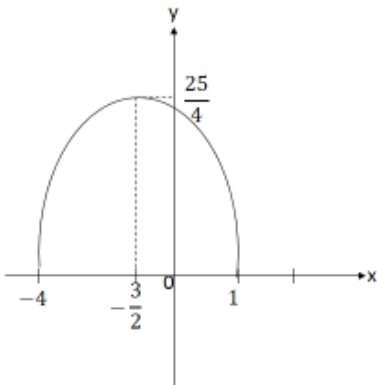
**MAJLIS PENGETUA SEKOLAH MALAYSIA (MPSM)
CAWANGAN KELANTAN**

**TINGKATAN 5
2020**

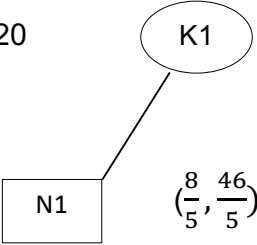
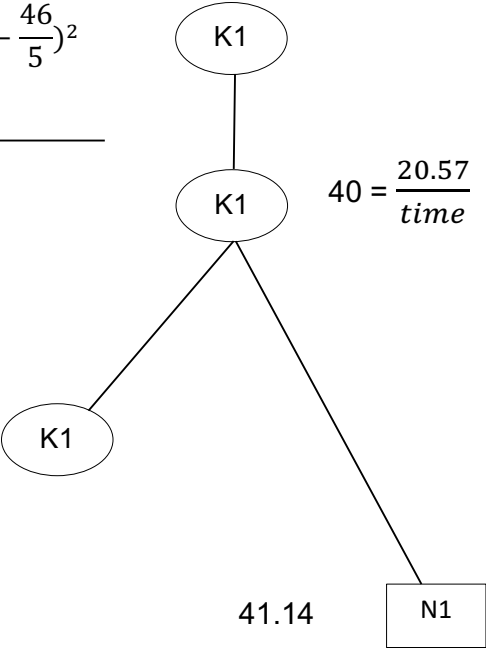
**ADDITIONAL MATHEMATICS
KERTAS 2**

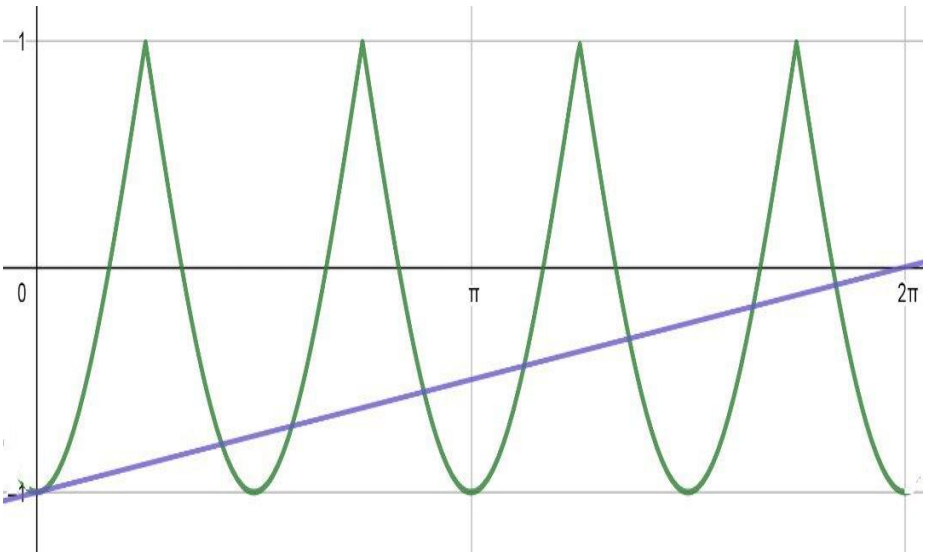
UNTUK KEGUNAAN PEMERIKSA SAHAJA

**SKEMA
PEMARKAHAN**

NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
1.	<p>(a) $f(x) = -(x^2 + 3x + (\frac{3}{2})^2 - (\frac{3}{2})^2 - 4)$ OR equivalent $f(x) = -(x + \frac{3}{2})^2 + \frac{25}{4}$</p> <div style="text-align: right;"> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">K1</div> <div style="display: flex; justify-content: space-around; width: 100px;"> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">K1</div> <div style="border: 1px solid black; padding: 5px; display: inline-block;">N1</div> </div> <p>$(-\frac{3}{2}, \frac{25}{4})$</p> </div> <p>(b)</p>  <p>Shape N1</p> <p>Maximum point N1</p> <p>X intercept N1</p> <p>(c) $0 \leq f(x) \leq \frac{25}{4}$ N1</p>	3	
			7

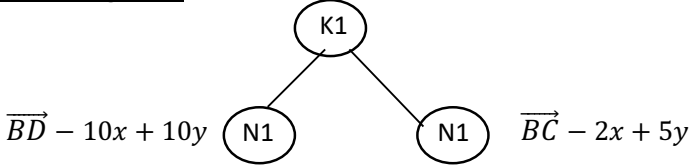
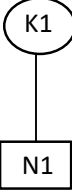

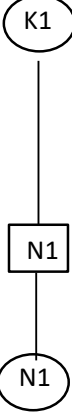
NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
2.	<p>(a) $T_7 = 100\pi \left(\frac{1}{2}\right)^{7-1}$</p> <p style="text-align: center;"> </p> <p style="text-align: right;">100π, 50π, 25π.</p> <p>(b) $100\pi \left(\frac{1}{2}\right)^{n-1} = \frac{25}{64}\pi$</p> <p style="text-align: center;"> </p> <p>(c) $\frac{100\pi}{1 - \frac{1}{2}}$</p> <p style="text-align: center;"> </p>	3	
		2	
		2	
			7

NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
3.	<p>(a) $x + 2(2x + 6) = 20$ or $\frac{y-6}{2} + 2y = 20$</p> <div style="text-align: right;">  </div> <p>(b)</p> <div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> $\sqrt{(20 - \frac{8}{5})^2 + (0 - \frac{46}{5})^2}$ <hr style="width: 25%; margin-left: 0;"/> <p>20.57</p> $80 = \frac{s}{0.5143}$ $t_p = t_Q$ </div> <div style="width: 45%;">  </div> </div>	2	4
			6

O	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
4	<p>(a)</p>  <p>Shape of $\cos 2x$ N1</p> <p>Max and min $y = -2\cos 2x$ N1</p> <p>2 cycles for $0 \leq x \leq 2\pi$ N1</p> <p>Modulus graph N1</p> <p>(b) $y = \frac{x}{2\pi} - 1$ N1</p> <p>Graph straight line $c=-1$ and m positive N1</p> <p>Number of solutions = 8 N1</p>	4	3
			7

NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
5	<p> $x - 3y + 4 = 5$ P1 </p> <p> $y(x + 2y) = 5$ P1 </p> <p> $x = 1 + 3y$ <u>or</u> $y = \frac{x-1}{3}$ P1 </p> <p> $y(1 + 3y + 2y) = 5$ <u>or</u> $\frac{x-1}{3} \left(x + 2 \left(\frac{x-1}{3} \right) \right) = 5$ K1 </p> <p style="text-align: right;"> Solve the quadratic equation Formulae $y = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(5)(-5)}}{2(5)}$ <u>or</u> $x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(5)(-43)}}{2(5)}$ </p> <p> <u>Or</u> $y = 0.905, y = -1.105$ N1 $x = 3.715, x = -2.315$ </p> <p> <u>Or</u> $x = 3.715, x = -2.315$ N1 $y = 0.905, y = -1.105$ </p>	7	7

NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
6(a)	$\frac{dV}{dt} = \frac{0.316 - 0.054}{25}$ <p style="text-align: center;">(K1)</p> $\frac{131}{12500} \text{ or } 0.01048$ <p style="text-align: center;">(N1)</p>	2	
6(b)	$\frac{dV}{dr} = 4\pi r^2 \text{ or } \frac{dA}{dr} = 8\pi r$ <p style="text-align: center;">(K1) (K1) Substitute $r = 1.2$</p> $\frac{dA}{dt} = \frac{dV}{dt} \times \frac{dA}{dr} \times \frac{dr}{dV}$ <p style="text-align: center;">(K1)</p> $\frac{131}{12500} \times 8\pi r \times \frac{1}{4\pi r^2}$ $\frac{131}{450} \text{ or } 0.2911$ <p style="text-align: center;">(N1)</p>	4	6

NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
7 (a)	<p>Write triangle law</p>  <p>$\vec{BD} = 10x + 10y$ $\vec{BC} = 2x + 5y$</p>	3	
(b)(i)	<p>$\vec{AC} = 8x + 5y$</p>  <p>$\vec{AF} = \frac{k}{1+k}(12x - 5y)$</p>		
(ii)	<p>$\vec{ED} = -4x + 10y$</p>  <p>$\vec{AF} = (4 - 4h)x + 10hy$</p>	4	
(c)	<p>Equate and solve coefficient of x or y</p> <p>$\frac{8k}{1+k} = 4 - 4h$ or $\frac{5k}{1+k} = 10h$</p>  <p>$k = \frac{2}{3}$</p> <p>$h = \frac{1}{5}$</p>	3	
			10

NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
8 (a)(i)	mean, $\mu = 500$ (N1)	1	
(ii)	$P(Z > \frac{m - 500}{100}) = 0.2$ (K1) <div style="text-align: center;"> </div> $\frac{m - 500}{100} = 0.842$ Ahmad qualify/ layak $585 > 584.2$ (N1)	4	
(b)(i)	$P\left(\frac{400 - 500}{100} \leq z \leq \frac{680 - 500}{100}\right)$ or $P(-1 \leq z \leq 1.8)$ (K1) <div style="text-align: center;"> </div> 0.80541 (N1)	2	
(ii)	$n = \frac{1252}{0.8054}$ (K1) <div style="text-align: center;"> </div> 0.2(1554) (K1) 310 / 311 (N1)	3	
			10

NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
9 (a)	$120^\circ \times \frac{\pi}{180^\circ}$ <div style="display: flex; align-items: center; justify-content: center;"> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; margin-right: 10px;">K1</div> <div style="border-left: 1px solid black; height: 20px; margin: 0 5px;"></div> <div style="border: 1px solid black; border-radius: 50%; padding: 5px;">N1</div> </div> $\frac{2\pi}{3}$	2	
(b)(i)	$\sin 60^\circ = \frac{x}{j}$ <div style="display: flex; align-items: center; justify-content: center;"> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; margin-right: 10px;">P1</div> <div style="border-left: 1px solid black; height: 20px; margin: 0 5px;"></div> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; margin-right: 10px;">K1</div> <div style="margin-left: 10px;">Use $2j \sin \frac{\theta}{2}$</div> </div> $2 \left[\frac{\sqrt{3}}{2} j \right]$ <div style="display: flex; align-items: center; justify-content: center;"> <div style="margin-right: 10px;">$\sqrt{3} j$</div> <div style="border: 1px solid black; padding: 5px;">N1</div> </div>	3	
(ii)	$\sin 60^\circ = \frac{\sqrt{3}}{2} \text{ or } \theta = \frac{\pi}{3} \text{ or } \theta = \frac{2\pi}{3}$ <div style="display: flex; align-items: center; justify-content: center;"> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; margin-right: 10px;">P1</div> </div> $A_1 = \pi j^2 \quad \text{or}$ $A_2 = \frac{1}{2} j^2 \left(\frac{2\pi}{3} \right)$ <div style="display: flex; align-items: center; justify-content: center;"> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; margin-right: 10px;">K1</div> <div style="border-left: 1px solid black; height: 20px; margin: 0 5px;"></div> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; margin-right: 10px;">K1</div> <div style="margin-left: 10px;">$A_3 = \frac{1}{2} j^2 \frac{\pi}{3} - \frac{1}{2} j^2 \frac{\sqrt{3}}{2}$</div> </div> $A_1 - A_2 - 2A_3$ <div style="display: flex; align-items: center; justify-content: center;"> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; margin-right: 10px;">K1</div> <div style="border-left: 1px solid black; height: 20px; margin: 0 5px;"></div> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; margin-right: 10px;">K1</div> <div style="margin-left: 10px;">$\frac{\pi j^2}{3} + \frac{\sqrt{3} j}{2}$</div> </div> <div style="display: flex; align-items: center; justify-content: center;"> <div style="margin-right: 10px;">$\frac{\pi j^2}{3} + \frac{\sqrt{3} j}{2}$</div> <div style="border: 1px solid black; padding: 5px;">N1</div> </div>	5	
			10

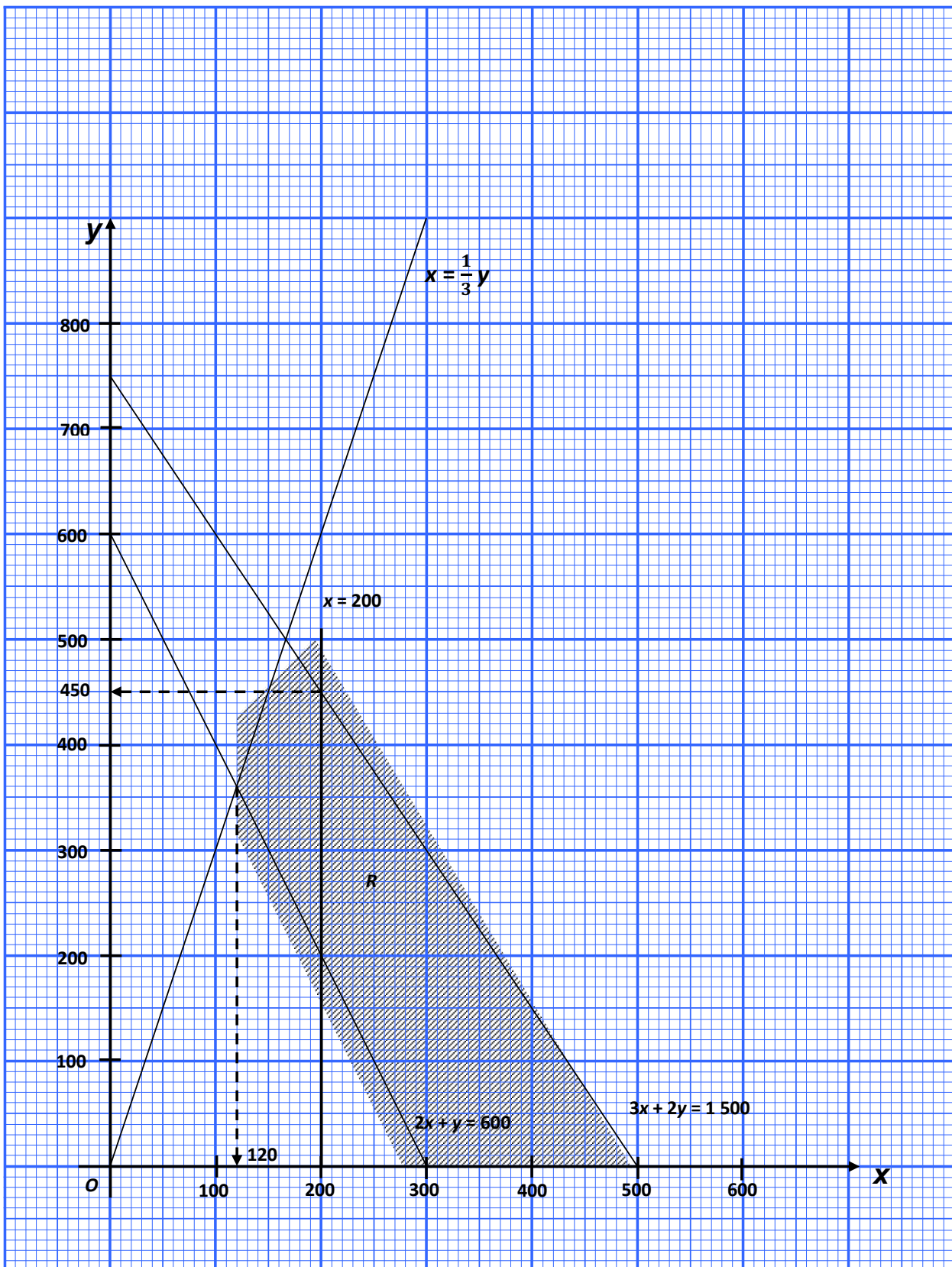
NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS														
10 (a)	<table border="1" data-bbox="149 324 1040 455"> <tr> <td>$\frac{1}{u}$</td> <td>0.80</td> <td>0.50</td> <td>0.33</td> <td>0.25</td> <td>0.21</td> <td>0.17</td> </tr> <tr> <td>$\frac{1}{v}$</td> <td>0.35</td> <td>1.60</td> <td>2.25</td> <td>2.55</td> <td>2.75</td> <td>2.90</td> </tr> </table>	$\frac{1}{u}$	0.80	0.50	0.33	0.25	0.21	0.17	$\frac{1}{v}$	0.35	1.60	2.25	2.55	2.75	2.90	<div style="border: 1px solid black; display: inline-block; padding: 2px;">N1</div> <div style="border: 1px solid black; display: inline-block; padding: 2px;">N1</div>	
$\frac{1}{u}$	0.80	0.50	0.33	0.25	0.21	0.17											
$\frac{1}{v}$	0.35	1.60	2.25	2.55	2.75	2.90											
(b)	<p>Plot $\frac{1}{v}$ against $\frac{1}{u}$ (Correct axes and uniform scales)</p> <p>6 *points plotted correctly</p> <p>Line of best fit (At least *5 points plotted)</p>	<div style="border: 1px solid black; display: inline-block; padding: 2px;">N1</div> <div style="border: 1px solid black; display: inline-block; padding: 2px;">N1</div> <div style="border: 1px solid black; display: inline-block; padding: 2px;">N1</div>	2 3														
(c)(i)	<p>$u = 2.33 \pm 0.1$ N1</p> <p>$\frac{1}{v} = \frac{2k}{hu} + \frac{9}{h}$ P1</p> <p>Use $c = \frac{9}{h}$ <u>or</u> $m = \frac{2k}{h}$</p> <p>$h = 2.54$ N1 $k = -5.14$ N1</p>	<div style="border: 1px solid black; display: inline-block; padding: 2px;">K1</div> <div style="border: 1px solid black; display: inline-block; padding: 2px;">N1</div> <div style="border: 1px solid black; display: inline-block; padding: 2px;">N1</div> <div style="border: 1px solid black; display: inline-block; padding: 2px;">K1</div> <div style="border: 1px solid black; display: inline-block; padding: 2px;">N1</div>	5														
			10														

NO	SOLUTION AND MARK SCHEME	SUB MARK S	TOTAL MARK S														
10	<p>The graph shows a linear relationship between $1/v$ (y-axis) and $1/u$ (x-axis). The y-axis ranges from 0 to 6.0 with major ticks every 0.5 and minor ticks every 0.1. The x-axis ranges from 0 to 0.9 with major ticks every 0.1 and minor ticks every 0.02. A straight line is plotted through the following data points:</p> <table border="1"> <thead> <tr> <th>$1/u$</th> <th>$1/v$</th> </tr> </thead> <tbody> <tr> <td>0.18</td> <td>2.9</td> </tr> <tr> <td>0.22</td> <td>2.8</td> </tr> <tr> <td>0.25</td> <td>2.6</td> </tr> <tr> <td>0.35</td> <td>2.3</td> </tr> <tr> <td>0.50</td> <td>1.6</td> </tr> <tr> <td>0.80</td> <td>0.4</td> </tr> </tbody> </table> <p>The line of best fit passes through the y-axis at approximately 3.6 and the x-axis at approximately 0.9.</p>	$1/u$	$1/v$	0.18	2.9	0.22	2.8	0.25	2.6	0.35	2.3	0.50	1.6	0.80	0.4		
$1/u$	$1/v$																
0.18	2.9																
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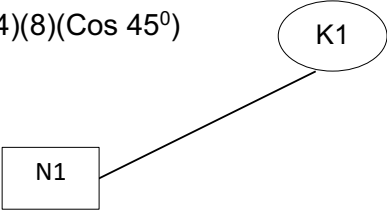
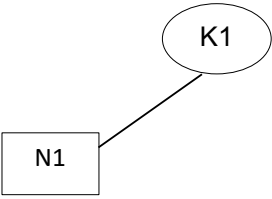
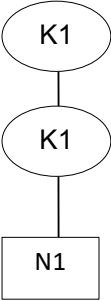
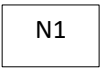
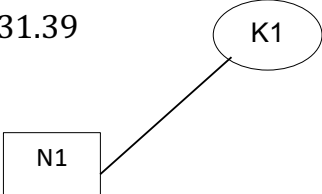
NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
11 (a)	$3 = 4 - \frac{x^2}{4}$ <p style="text-align: center;">(K1)</p> $x = 2, x = -2$ <p style="text-align: center;">(N1)</p> $BC = 4$ <p style="text-align: center;">(N1)</p>	3	
(b)	$\int_{-2}^2 \left[4 - \frac{x^2}{4}\right] dx$ <p style="text-align: center;">(K1)</p> $\left[4x - \frac{x^3}{12}\right]_{-2}^2$ <p style="text-align: center;">(K1)</p> $\left[4(2) - \frac{2^3}{12}\right] - \left[4(-2) - \frac{(-2)^3}{12}\right]$ <p style="text-align: center;">(K1)</p> $14.67 \text{ or } \frac{44}{3}$ <p style="text-align: center;">(N1)</p>	4	
(c)	$4(1)$ <p style="text-align: center;">(K1)</p> $18.67 \text{ or } \frac{56}{3}$ <p style="text-align: center;">(N1)</p> <p style="text-align: right;">$\frac{44}{3} + 4(1)$</p> <p style="text-align: right;">(K1)</p>	3	10

NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
12	<p>(a) $r = 6$ P1</p> <p style="text-align: right;">substitute $t=3$ in equation V</p> <hr/> <p style="text-align: right;">$p(3)^2 + q(3) + 6 = 42$ K1</p> <p>$\frac{dv}{dt} = 2pt + q$ K1</p> <p style="text-align: right;">$9p + 3q = 36$ OR $6p + q = 0$ K1</p> <p>$p = -4$ and $q = 24$ N1</p> <p>(b)</p> <p>$t = \frac{-(-24) \pm \sqrt{(24)^2 - 4(-4)(6)}}{2(-4)}$</p> <hr/> <p>$-4t^2 + 24t + 6 = 0$</p> <p style="text-align: right;">$t = 3 + \frac{1}{8}\sqrt{672}$ K1 N1</p> <p>(c)</p> <p>$s = \frac{4}{3}t^3 + \frac{24}{2}t^2 + 6t$ K1</p> <p>S</p> <p style="text-align: right;">substitute $t = 6$ or $t = 5$ in equation</p> <hr/> <p style="text-align: right;">$s = \frac{4}{3}(6)^3 + \frac{24}{2}(6)^2 + 6(6)$ or</p> <p style="text-align: right;">$s = \frac{4}{3}(5)^3 + \frac{24}{2}(5)^2 + 6(5)$ K1</p> <p>$\frac{778}{3}$ N1</p>	<p>5</p> <p>2</p> <p>3</p>	<p></p> <p></p> <p>10</p>

NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
13.	<p>a)</p> <p>(i) $x \geq \frac{1}{3}y$ or $y \leq 3x$ N1</p> <p>(ii) $12x + 8y \leq 6000$ or $3x + 2y \leq 1500$ N1</p> <p>(iii) $8x + 4y \geq 2400$ or $2x + y \geq 600$ N1</p> <p>(b) graph- attachment</p> <p>- draw correctly at least one straight line from * inequalities involves x and y K1</p> <p>- draw correctly ALL the * straight line N1</p> <p>Note: Accept dotted line</p> <p>Region shaded correctly. N1</p> <p>(c)</p> <p>(i) 120 N1</p> <p>(ii) (200, 450) N1 seen 450</p> <div style="margin-left: 100px;"> $\frac{8(200) + 4(450)}{8x + 4y \text{ (profit equation)}}$ </div> <div style="margin-left: 400px; margin-top: 20px;"> K1 </div> <div style="margin-left: 300px; margin-top: 40px;"> N1 </div> <p style="margin-left: 300px;">RM 3400.00</p> <p>Noted: inequality for which no symbol "=" is accepted</p>	3	10
		3	
		4	



NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
14.	<p>(a)</p> <p>(i) $135 = \frac{210}{Q_{2018}} \times 100$</p> <p>RM 155.56</p> <p style="text-align: right;">K1</p> <p style="text-align: center;">N1</p> <p>(ii) $\frac{120}{100} \times \frac{130}{100} \times 100$</p> <p>156</p> <p>Increase 56 %</p> <p style="text-align: right;">K1</p> <p style="text-align: center;">N1</p> <p style="text-align: center;">N1</p> <p>(b)</p> <p>(i) $p = 15$</p> <p style="text-align: center;">N1</p> $\frac{(135 \times 50) + (y \times 25) + (120 \times 15) + (70 \times 10)}{50 + 25 + p + (p - 5)} = 119.50$ <p style="text-align: right;">K1</p> <p>108</p> <p style="text-align: center;">N1</p> <p>(ii) $108 = \frac{Q_{2020}}{130} \times 100$</p> <p>RM 140.40</p> <p style="text-align: right;">K1</p> <p style="text-align: center;">N1</p>	<p>2</p> <p>3</p> <p>3</p> <p>2</p>	<p>10</p>

NO	SOLUTION AND MARK SCHEME	SUB MARKS	TOTAL MARKS
15. (a)	<p>(i) $BD^2 = 3.74^2 + 8^2 - 2(3.74)(8)(\cos 45^\circ)$</p> <p>5.973 km</p>  <p>(ii) $\frac{\sin \angle ACD}{8} = \frac{\sin 45^\circ}{7.85}$</p> <p>46.11°</p> <p>Noted: $\angle ACD = \angle BCD$</p>  <p>(iii)</p> <p>$A = \frac{1}{2} \times 8 \times 7.85 \times \sin 88.89^\circ$</p> <p>31.39 km²</p> 	2 2 3	
(b)	<p>The farthest hotel from hotel A is hotel C because the distance between them faces the largest angle</p> 	1	
(c)	<p>$\frac{1}{2} \times 8 \times (\text{shortest distance}) = 31.39$</p> <p>7.848 km</p> 	2	10