

Nama: .....

Kelas: .....

3472/1

**SULIT**

3472/1

Matematik

Tambahan

Kertas 1

November

2023

2 jam



## MAKTAB RENDAH SAINS MARA

### PEPERIKSAAN AKHIR SIJIL PENDIDIKAN MRSM 2023

#### MATEMATIK TAMBAHAN

Kertas 1

Dua jam

#### JANGAN BUKA KERTAS PEPERIKSAAN INI SEHINGGA DIBERITAHU

1. Tulis nama dan kelas anda pada ruang yang disediakan.
2. Kertas peperiksaan ini adalah dalam dwibahasa.
3. Soalan dalam bahasa Melayu mendahului soalan yang sepadan dalam bahasa Inggeris.
4. Calon dibenarkan menjawab keseluruhan atau sebahagian soalan sama ada dalam bahasa Melayu atau bahasa Inggeris.
5. Calon dikehendaki membaca maklumat di halaman belakang kertas peperiksaan ini.

Bahagian	Soalan	Markah Penuh	Markah Diperoleh
A	1	3	
	2	2	
	3	5	
	4	5	
	5	5	
	6	6	
	7	6	
	8	8	
	9	5	
	10	6	
	11	8	
	12	5	
B	13	8	
	14	8	
	15	8	
Jumlah		80	

Kertas peperiksaan ini mengandungi 36 halaman bercetak.

[Lihat halaman sebelah

Rumus-rumus berikut boleh membantu anda menjawab soalan. Simbol-simbol yang diberi adalah yang biasa digunakan.

*The following formulae may be helpful in answering the questions. The symbols given are the ones commonly used.*

$$1. \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$2. \quad a^m \times a^n = a^{m+n}$$

$$3. \quad a^m \div a^n = a^{m-n}$$

$$4. \quad (a^m)^n = a^{mn}$$

$$5. \quad \log_a mn = \log_a m + \log_a n$$

$$6. \quad \log_a \left( \frac{m}{n} \right) = \log_a m - \log_a n$$

$$7. \quad \log_a m^n = n \log_a m$$

$$8. \quad \log_a b = \frac{\log_c b}{\log_c a}$$

$$9. \quad T_n = a + (n-1)d$$

$$10. \quad S_n = \frac{n}{2} [2a + (n-1)d]$$

$$11. \quad T_n = ar^{n-1}$$

$$12. \quad S_n = \frac{a(r^n - 1)}{r-1} = \frac{a(1 - r^n)}{1-r}, r \neq 1$$

$$13. \quad S_\infty = \frac{a}{1-r}, |r| < 1$$

$$14. \quad y = uv, \quad \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$15. \quad y = \frac{u}{v}, \quad \frac{dy}{dx} = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

$$16. \quad \frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$$

$$17. \quad \text{Luas di bawah lengkung} \\ \text{Area under a curve}$$

$$= \int_a^b y \, dx \text{ atau (or)}$$

$$= \int_a^b x \, dy$$

$$18. \quad \text{Isi padu janaan}$$

*Volume generated*

$$= \int_a^b \pi y^2 \, dx \text{ atau (or)}$$

$$= \int_a^b \pi x^2 \, dy$$

$$19. \quad I = \frac{Q_1}{Q_0} \times 100$$

$$20. \quad \bar{I} = \frac{\sum W_i I_i}{\sum W_i}$$

$$21. \quad {}^n P_r = \frac{n!}{(n-r)!}$$

$$22. \quad {}^n C_r = \frac{n!}{(n-r)!r!}$$

$$23. \quad P(X = r) = {}^n C_r p^r q^{n-r}, \quad p + q = 1$$

$$24. \quad \text{Min / Mean}, \quad \mu = np$$

$$25. \quad \sigma = \sqrt{npq}$$

$$26. \quad Z = \frac{X - \mu}{\sigma}$$

$$27. \quad \text{Panjang lengkok}, \quad s = j\theta \\ \text{Arc length}, \quad s = r\theta$$

$$28. \quad \text{Luas sektor}, \quad L = \frac{1}{2} j^2 \theta$$

$$\text{Area of sector}, \quad A = \frac{1}{2} r^2 \theta$$

$$29. \quad \sin^2 A + \cos^2 A = 1$$

$$\sin^2 A + \cos^2 A = 1$$

$$30. \quad \operatorname{sek}^2 A = 1 + \tan^2 A$$

$$\sec^2 A = 1 + \tan^2 A$$

$$31. \quad \operatorname{kosek}^2 A = 1 + \cot^2 A$$

$$\cosec^2 A = 1 + \cot^2 A$$

32.  $\sin 2A = 2 \sin A \cos A$

$$\sin 2A = 2 \sin A \cos A$$

33.  $\cos 2A = \cos^2 A - \sin^2 A$

$$= 2 \cos^2 A - 1$$

$$= 1 - 2 \sin^2 A$$

$$\cos 2A = \cos^2 A - \sin^2 A$$

$$= 2 \cos^2 A - 1$$

$$= 1 - 2 \sin^2 A$$

34.  $\tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$

35.  $\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

36.  $\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

37.  $\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$

38.  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

39.  $a^2 = b^2 + c^2 - 2bc \cos A$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

40. Luas segi tiga / Area of triangle

$$= \frac{1}{2} ab \sin C$$

41. Titik yang membahagi suatu tembereng garis

A point dividing a segment of a line

$$(x, y) = \left( \frac{nx_1 + mx_2}{m+n}, \frac{ny_1 + my_2}{m+n} \right)$$

42. Luas segi tiga / Area of triangle

$$= \frac{1}{2} |(x_1y_2 + x_2y_3 + x_3y_1) - (x_2y_1 + x_3y_2 + x_1y_3)|$$

43.  $|\mathbf{r}| = \sqrt{x^2 + y^2}$

44.  $\hat{\mathbf{r}} = \frac{x\mathbf{i} + y\mathbf{j}}{\sqrt{x^2 + y^2}}$

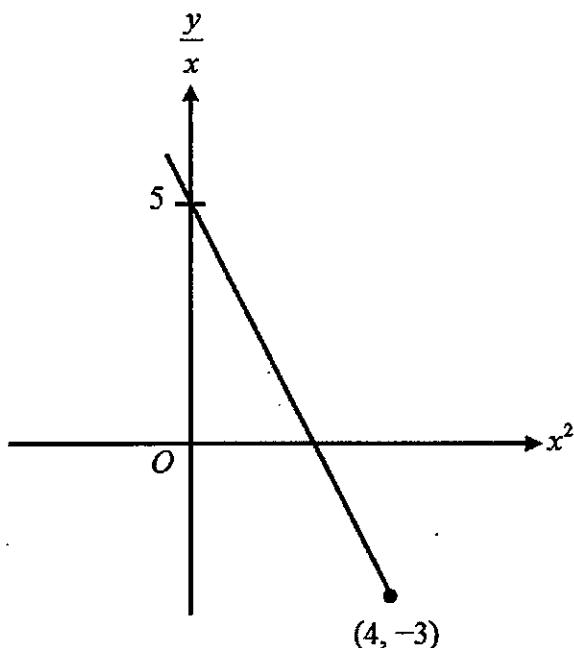
**Bahagian A**

[64 markah]

*Jawab semua soalan.*

- 1 Rajah 1 menunjukkan satu graf garis lurus  $\frac{y}{x}$  melawan  $x^2$ .

*Diagram 1 shows a straight line graph  $\frac{y}{x}$  against  $x^2$ .*



Rajah 1

Diagram 1

Ungkapkan  $y$  dalam sebutan  $x$ .

[3 markah]

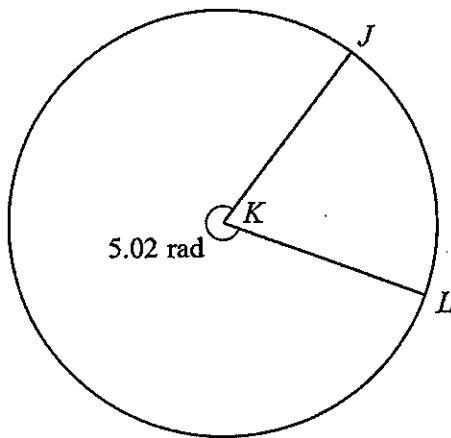
Express  $y$  in terms of  $x$ .

[3 marks]

Jawapan / Answer:

- 2 Rajah 2 menunjukkan lengkok  $JL$  yang mencangkum sudut 5.02 rad pada pusat bulatan  $K$ . Jejari bulatan itu ialah 12.5 cm.

*Diagram 2 shows an arc  $JL$  which subtends an angle of 5.02 rad at the centre of the circle  $K$ . The radius of the circle is 12.5 cm.*



Rajah 2  
Diagram 2

Cari luas, dalam  $\text{cm}^2$ , sektor minor  $JKL$ .

[2 markah]

*Find the area, in  $\text{cm}^2$ , of minor sector  $JKL$ .*

[2 marks]

[Guna / Use  $\pi = 3.142$ ]

Jawapan / Answer:

- 3 Diberi  $A(4, 20)$  berada di atas suatu lengkung  $y = -2x^2 + 10x + 12$ , cari  
*Given  $A(4, 20)$  lies on a curve  $y = -2x^2 + 10x + 12$ , find*

- (a) kecerunan tangen kepada lengkung pada titik  $A$ , [2 markah]  
*the gradient of tangent to the curve at point A,* [2 marks]
- (b) persamaan normal kepada lengkung pada titik  $A$ . [3 markah]  
*the equation of normal to the curve at point A.* [3 marks]

Jawapan / Answer:

- 4 Encik Adi, Puan Balqis dan Encik Chandran merupakan 3 orang ahli generasi pertama dalam sebuah pertubuhan. Perlembagaan pertubuhan menetapkan bahawa setiap ahli dikehendaki merekrut 2 orang ahli baharu.

*Encik Adi, Puan Balqis and Encik Chandran are 3 members of the first generation in an organization. The constitution of the organization stipulates that each member needs to recruit 2 new members.*

[Anggapkan bahawa setiap ahli pada setiap generasi berjaya memenuhi perlembagaan pertubuhan]

[Assume that each member has successfully fulfilled the constitution of the organization]

- (a) Jika jumlah ahli pertubuhan itu melebihi 12 000 orang kali pertama pada generasi ke- $n$ , cari nilai  $n$ . [2 markah]

*If the total members of the organization exceed 12 000 for the first time in the  $n^{\text{th}}$  generation, find the value of  $n$ .* [2 marks]

- (b) Seterusnya, cari beza antara jumlah ahli pertubuhan itu sehingga generasi ke- $n$  dengan bilangan ahli pada generasi ke- $n$ . [3 markah]

*Hence, find the difference between the total members of the organization until the  $n^{\text{th}}$  generation and the number of members in the  $n^{\text{th}}$  generation.* [3 marks]

Jawapan / Answer:

[Lihat halaman sebelah  
SULIT]

- 5 (a) Cari julat nilai  $x$  bagi ketaksamaan kuadratik  $-x^2 < \frac{1}{2}(x-1)$ . [3 markah]  
*Find the range of values of  $x$  for the quadratic inequality  $-x^2 < \frac{1}{2}(x-1)$ .* [3 marks]

Jawapan / Answer:

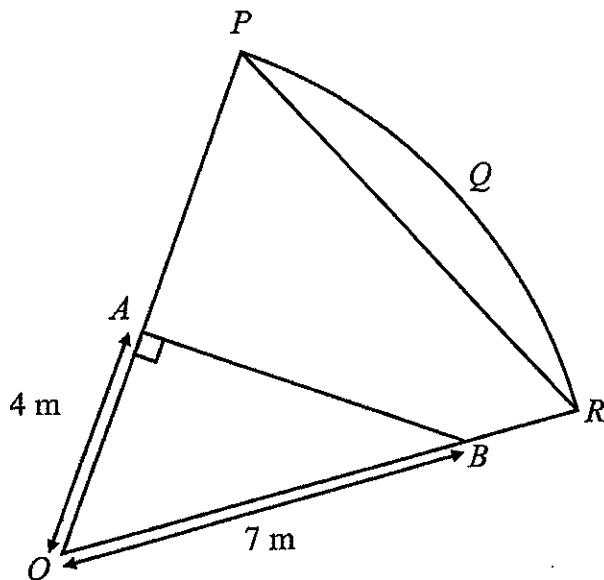
- (b) Diberi  $ax^2 + bx + c = 0$ , terbitkan rumus kuadratik dengan menggunakan kaedah penyempurnaan kuasa dua. [2 markah]

*Given  $ax^2 + bx + c = 0$ , derive the quadratic formula by using completing the square method.* [2 marks]

Jawapan / Answer:

- 6 Rajah 3 menunjukkan segi tiga  $AOB$  dan tembereng  $PQR$  yang terterap dalam sektor  $POR$  dengan pusat  $O$ .

*Diagram 3 shows triangle  $AOB$  and segment  $PQR$  inscribed in sector  $POR$  with centre  $O$ .*



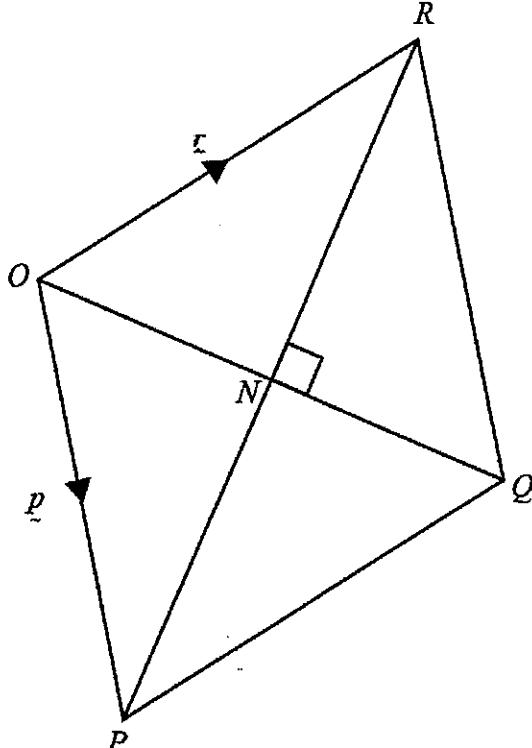
Rajah 3  
Diagram 3

- (a) Tunjukkan bahawa  $\angle AOB = 0.963$  rad. [2 markah]  
*Show that  $\angle AOB = 0.963$  rad.* [2 marks]  
*[Guna / Use  $\pi = 3.142$ ]*
- (b) Diberi perimeter tembereng  $PQR$  adalah lebih kecil daripada perimeter segi tiga  $AOB$ , cari julat bagi jejari sektor tersebut. [4 markah]  
*Given the perimeter of segment  $PQR$  is less than the perimeter of triangle  $AOB$ , find the range of the radius of the sector.* [4 marks]

Jawapan / Answer:

- 7 Rajah 4 menunjukkan rombus  $OPQR$  dengan  $\angle ORQ = 60^\circ$ . Pepenjuru  $OQ$  dan  $PR$  bersilang pada titik  $N$ .

*Diagram 4 shows rhombus  $OPQR$  with  $\angle ORQ = 60^\circ$ . The diagonals  $OQ$  and  $PR$  intersect at point  $N$ .*



Rajah 4  
Diagram 4

Diberi bahawa  $\overrightarrow{OP} = \underline{p}$ ,  $\overrightarrow{OR} = \underline{r}$  dan  $|\underline{p}| = 2$ .

*It is given that  $\overrightarrow{OP} = \underline{p}$ ,  $\overrightarrow{OR} = \underline{r}$  and  $|\underline{p}| = 2$ .*

- (a) Nyatakan magnitud bagi  $3\overrightarrow{QR}$ .

[1 markah]

*State the magnitude of  $3\overrightarrow{QR}$ .*

[1 mark]

- (b) Ungkapkan dalam sebutan  $\underline{p}$  dan  $\underline{r}$ ,

*Express in terms of  $\underline{p}$  and  $\underline{r}$ ,*

(i)  $\overrightarrow{OQ}$

(ii)  $\overrightarrow{RN}$

[3 markah]

[3 marks]

- (c) Cari nilai bagi  $|\underline{p} - \underline{r}|$ .

[2 markah]

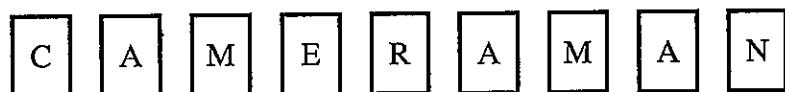
*Find the value of  $|\underline{p} - \underline{r}|$ .*

[2 marks]

Jawapan / Answer:

[Lihat halaman sebelah  
**SULIT**

- 8 (a) Rajah 5 menunjukkan sembilan keping kad huruf.  
*Diagram 5 shows nine letter cards.*



Rajah 5  
*Diagram 5*

Tiga keping kad huruf dipilih secara rawak.  
Cari bilangan cara memilih kad-kad itu jika tiga kad tersebut mengandungi

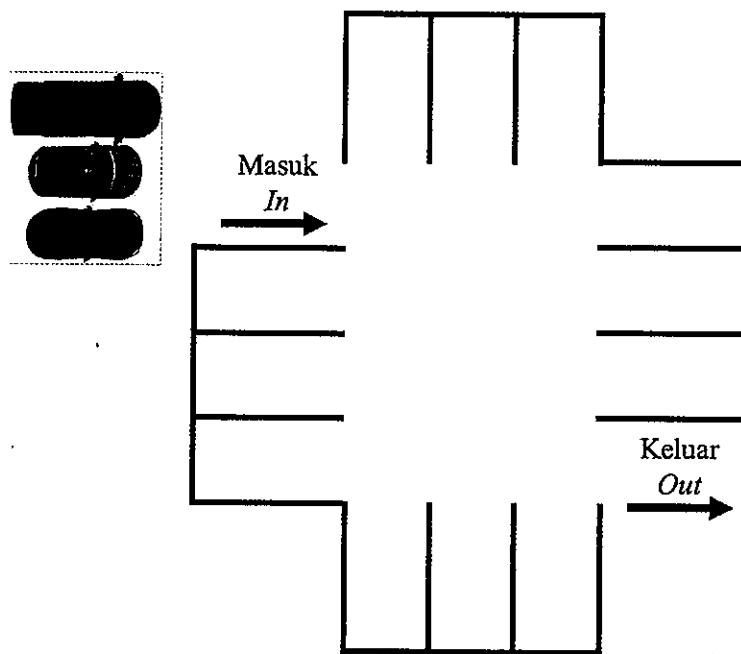
*Three letter cards are chosen at random.*  
*Find the number of ways to choose the cards if the three cards include*

- (i) tepat satu huruf M dan satu huruf A,  
*exactly one letter M and exactly one letter A,*
- (ii) sekurang-kurangnya satu huruf M.  
*at least one letter M.*

[4 markah]  
[4 marks]

Jawapan / Answer:

- (b) Rajah 6 menunjukkan 12 petak parkir kereta di sebuah kawasan.  
*Diagram 6 shows 12 car parking spaces in an area.*



Rajah 6  
*Diagram 6*

Terdapat 3 buah kereta perlu diparkir secara rawak di kawasan itu.  
Cari bilangan susunan kereta yang mungkin jika

*There are 3 cars need to be parked randomly in that area.  
Find the number of possible arrangements of the cars if*

- (i) tiada syarat dikenakan,  
*there is no restriction,*
- (ii) tiada kereta yang diparkir sebelah menyebelah.  
*none of the cars are parked next to each other.*

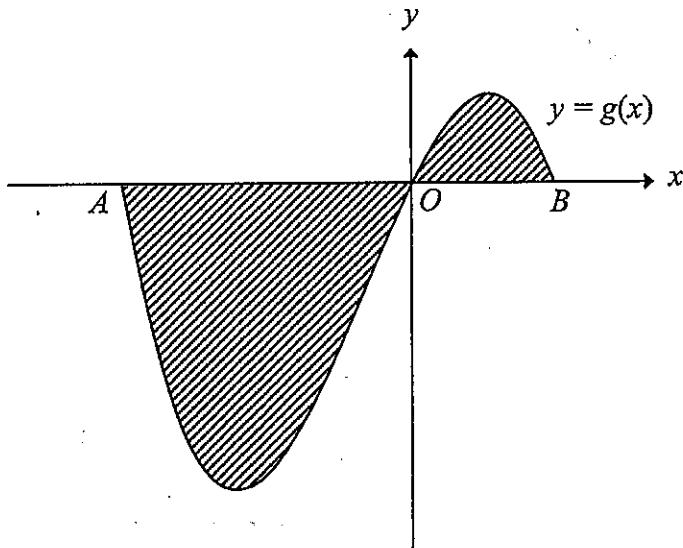
[4 markah]  
[4 marks]

Jawapan / Answer:

[Lihat halaman sebelah  
**SULIT**

- 9 Rajah 7 menunjukkan lengkung  $y = g(x)$  menyilang paksi- $x$  pada titik  $A$ , asalan dan titik  $B$ .

*Diagram 7 shows the curve  $y = g(x)$  intersects the  $x$ -axis at point A, origin and point B.*



Rajah 7  
Diagram 7

Diberi bahawa fungsi kecerunan bagi lengkung itu ialah  $-3x^2 - 2x + 2$ , cari

*Given that the gradient function of the curve is  $-3x^2 - 2x + 2$ , find*

- |   |                         |
|---|-------------------------|
| <p>(a) persamaan lengkung itu,<br/><i>the equation of the curve,</i></p>    | [1 markah]<br>[1 mark]  |
| <p>(b) luas kawasan berlorek.<br/><i>the area of the shaded region.</i></p> | [4 markah]<br>[4 marks] |

**Jawapan / Answer:**

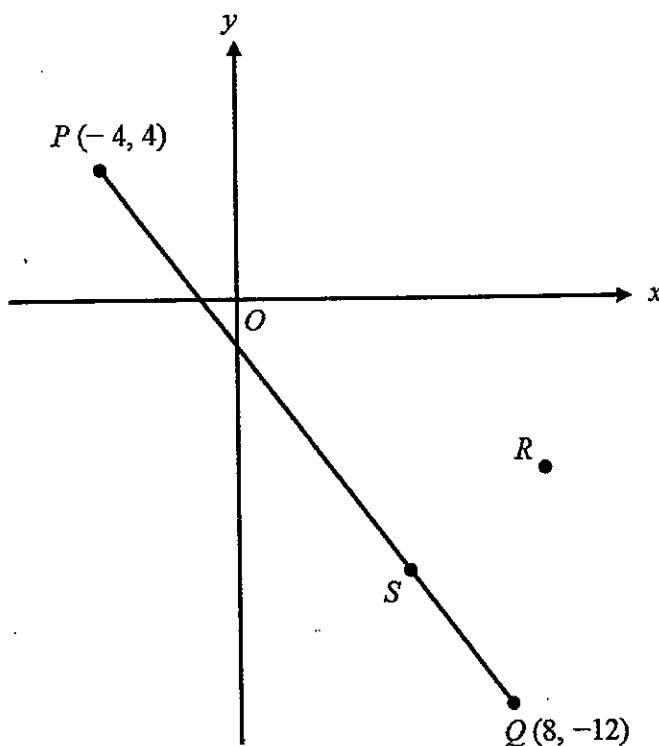
*[Lihat halaman sebelah*  
**SULIT**

- 10** Penyelesaian secara lukisan berskala **tidak** diterima.

*Solutions by scale drawing is not accepted.*

Rajah 8 menunjukkan suatu tembereng garis  $PQ$ .

*Diagram 8 shows a line segment  $PQ$ .*



Rajah 8  
Diagram 8

- (a) Diberi bahawa titik  $S$  berada di atas tembereng garis  $PQ$  dengan keadaan jaraknya dari titik  $P$  adalah 75% dari panjang  $PQ$ .

Cari koordinat  $S$ .

[3 markah]

*It is given that point  $S$  lies on the line segment  $PQ$  such that its distance from point  $P$  is 75% of length  $PQ$ .*

*Find the coordinates of  $S$ .*

[3 marks]

- (b) Jarak terdekat dari titik  $R$  ke tembereng garis  $PQ$  adalah melalui titik  $S$ .

Cari persamaan garis lurus  $RS$ .

[3 markah]

*The shortest distance from point  $R$  to the line segment  $PQ$  is through point  $S$ .*

*Find the equation of the straight line  $RS$ .*

[3 marks]

**Jawapan / Answer:**

*[Lihat halaman sebelah*  
**SULIT**

- 11 (a) Berikut adalah pernyataan palsu berkenaan janjang aritmetik.

*The following is a false statement regarding arithmetic progression.*

Janjang aritmetik ialah suatu jujukan nombor dengan setiap sebutan diperoleh dengan mendarabkan satu pemalar kepada sebutan sebelumnya.

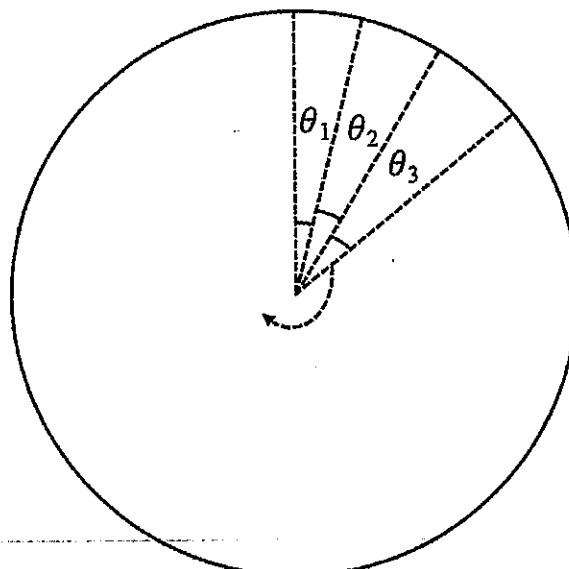
*Arithmetic progression is a sequence of numbers such that each terms is obtained by multiplying a constant to the term before it.*

Tuliskan satu pernyataan yang benar bagi janjang aritmetik dengan mengubah satu perkataan sahaja dari pernyataan itu. [1 markah]

*Write a true statement for an arithmetic progression by changing only one word from the statement. [1 mark]*

- (b) Rajah 9 menunjukkan sebuah bulatan yang akan dibahagikan kepada 15 sektor untuk membentuk suatu janjang aritmetik dengan keadaan  $\theta_1 < \theta_2$ .

*Diagram 9 shows a circle that will be divided into 15 sectors to form an arithmetic progression such that  $\theta_1 < \theta_2$ .*



Rajah 9

Diagram 9

- (i) Diberi bahawa sudut sektor terbesar ialah  $38^\circ$ , cari hasil tambah lima sebutan terakhir janjang itu.

*Given that the angle of the largest sector is  $38^\circ$ , find the sum of the last five terms of the progression.*

- (ii) Terdapat beberapa cara lain untuk membahagikan bulatan tersebut kepada 15 sektor. Cari semua padanan sebutan pertama,  $a$  dan beza sepunya,  $d$  dengan keadaan  $a$  dan  $d$  ialah integer positif.

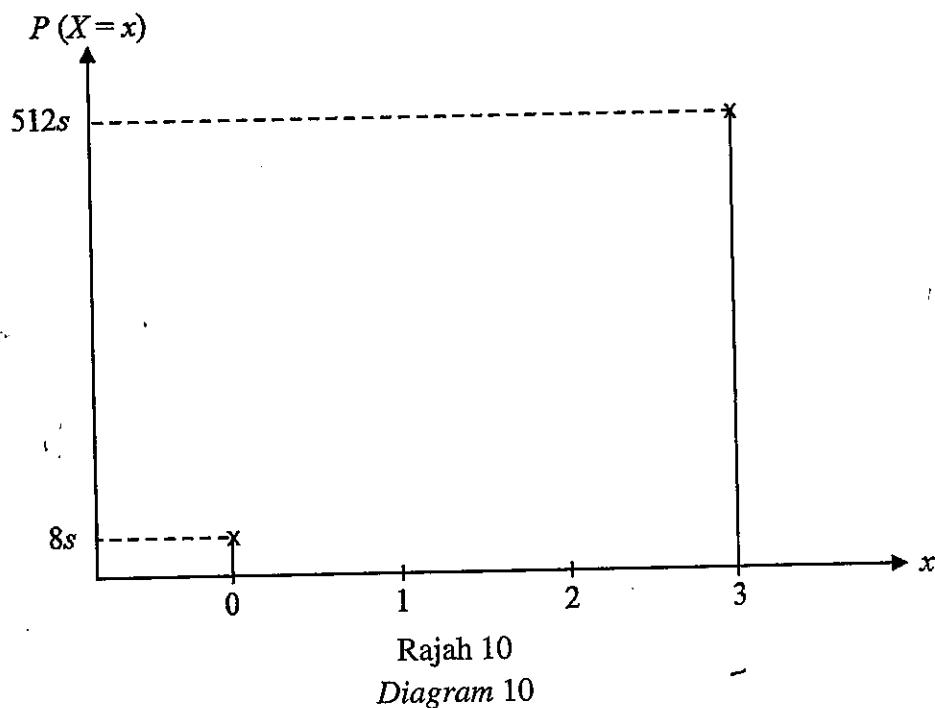
*There are other ways to divide the circle into 15 sectors. Find all the combination of the first term,  $a$  and the common difference,  $d$  such that  $a$  and  $d$  are positive integers.*

[7 markah]

[7 marks]

**Jawapan / Answer:**

- 12** Rajah 10 menunjukkan graf  $X \sim B(3, p)$  yang tidak lengkap.  
*Diagram 10 shows an incomplete graph of  $X \sim B(3, p)$ .*



- (a) Tunjukkan bahawa  $p = \sqrt[3]{s}$ . [2 markah]  
*Show that  $p = \sqrt[3]{s}$ .* [2 marks]
- (b) Cari nilai bagi  $P(X = 2)$ . [3 markah]  
*Find the value of  $P(X = 2)$ .* [3 marks]

Jawapan / Answer:

**Bahagian B**

[16 markah]

*Bahagian ini mengandungi tiga soalan. Jawab dua soalan.*

- 13** Diberi bahawa  $g(x) = \frac{x+4}{3}$  dan  $fg(x) = \frac{18}{17-x}$ ,  $x \neq k$ , cari

*Given that  $g(x) = \frac{x+4}{3}$  and  $fg(x) = \frac{18}{17-x}$ ,  $x \neq k$ , find*

- (a) (i) nilai  $k$ ,  
*the value of  $k$ ,*
- (ii)  $g(5)$ ,
- (iii) nilai  $x$  apabila  $g(x)$  memeta kepada diri sendiri.  
*the value of  $x$  when  $g(x)$  maps onto itself.*

[4 markah]  
[4 marks]

- (b) Cari  $f(x)$  dalam sebutan  $x$ . [2 markah]  
*Find  $f(x)$  in terms of  $x$ .* [2 marks]

- (c) Seterusnya, dengan menggunakan fungsi gubahan, sahkan bahawa  $h(x) = 7 - \frac{6}{x}$  adalah fungsi songsang bagi  $f(x)$ . [2 markah]

*Hence, by using composite function, verify that  $h(x) = 7 - \frac{6}{x}$  is the inverse function of  $f(x)$ .* [2 marks]

Jawapan / Answer:

14 (a) Sebuah silinder mempunyai jejari  $\left(\frac{1}{\sqrt{3}+1}\right)$  cm dan tinggi  $(\sqrt{3}-1)$  cm.

Cari isipadu silinder itu dalam bentuk  $(a+b\sqrt{3})\pi$  cm<sup>3</sup>, dengan keadaan  $a$  dan  $b$  ialah pemalar. [4 markah]

A cylinder has a radius of  $\left(\frac{1}{\sqrt{3}+1}\right)$  cm and a height of  $(\sqrt{3}-1)$  cm.

Find the volume of the cylinder in the form of  $(a+b\sqrt{3})\pi$  cm<sup>3</sup>, such that  $a$  and  $b$  are constants. [4 marks]

Jawapan / Answer:

- (b) Jadual 1 menunjukkan bilangan populasi di sebuah negara.

*Table 1 shows the number of population in a country.*

Tahun Year	Bilangan Populasi <i>Number of Population</i>
2020	33 200 000
2022	33 900 000

Jadual 1

*Table 1*

Kadar pertumbuhan populasi,  $r$  di negara itu boleh diwakili oleh  $r = \frac{1}{n} \ln \left( \frac{P_n}{P_0} \right)$

dengan keadaan  $P_n$  adalah bilangan populasi pada tahun semasa,  $P_0$  adalah bilangan populasi pada tahun asas dan  $n$  adalah bilangan tahun.

Cari kadar pertumbuhan, dalam peratus, bagi tahun 2022.

[2 markah]

*Population growth rate,  $r$  in the country can be represented by  $r = \frac{1}{n} \ln \left( \frac{P_n}{P_0} \right)$*

*such that  $P_n$  is the number of population in the current year,  $P_0$  is the number of population in the base year and  $n$  is the number of years.*

*Find the growth rate, in percentage, for the year 2022.*

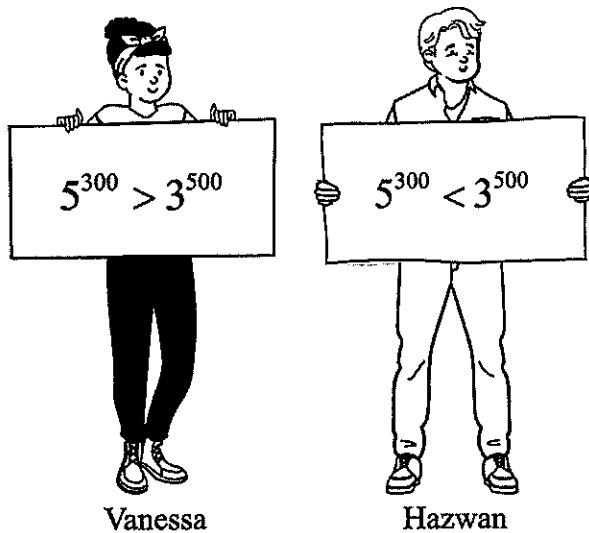
[2 marks]

Jawapan / Answer:

*[Lihat halaman sebelah*

- (c) Rajah 11 menunjukkan Vanessa dan Hazwan yang sedang memegang sepanduk.

*Diagram 11 shows Vanessa and Hazwan who are holding placards.*



Rajah 11

*Diagram 11*

Pernyataan siapakah yang benar?

Berikan justifikasi anda dengan menggunakan hukum indeks.

[2 markah]

*Whose statement is true?*

*Give your justification by using the law of indices.*

[2 marks]

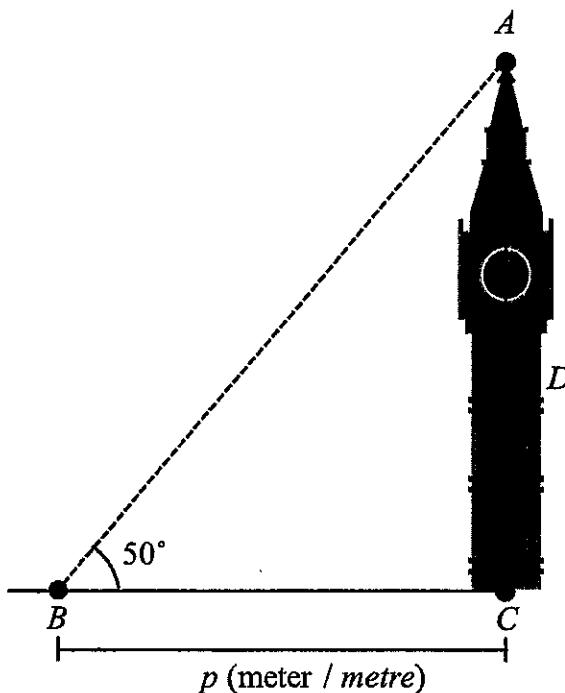
Jawapan / Answer:

- 15 (a) Selesaikan persamaan  $21 \cos^2 x = 8 \sin x + 16$  untuk  $0^\circ \leq x \leq 360^\circ$ . [4 markah]  
*Solve the equation  $21\cos^2 x = 8\sin x + 16$  for  $0^\circ \leq x \leq 360^\circ$ . [4 marks]*

Jawapan / Answer:

- (b) Rajah 12 menunjukkan sebuah menara jam tegak dengan ketinggian  $h$  meter di atas tanah mengufuk. Sebuah lampu limpah berada pada titik  $D$  dengan keadaan sudut dongakan  $D$  dari  $B$  ialah  $25^\circ$ .

*Diagram 12 shows a vertical clock tower with height of  $h$  metres on a horizontal ground. A spotlight is at point D such that the angle of elevation of D from B is  $25^\circ$ .*



Rajah 12  
Diagram 12

Ungkapkan  $\tan 25^\circ$  dalam sebutan  $h$  dan  $p$ .

[4 markah]

Express  $\tan 25^\circ$  in terms of  $h$  and  $p$ .

[4 marks]

**Jawapan / Answer:**

• **KERTAS SOALAN TAMAT**

**HALAMAN KOSONG**

**HALAMAN KOSONG**

*[Lihat halaman sebelah*  
**SULIT**

**HALAMAN KOSONG**

## THE UPPER TAIL PROBABILITY Q(z) FOR THE NORMAL DISTRIBUTION N(0,1) KEBARANGKALIAN HUJUNG ATAS Q(z) BAGI TABURAN NORMAL N(0,1)

<b>z</b>	<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>TOLAK</b>	
<b>0.0</b>	<b>.5000</b>	<b>.4960</b>	<b>.4920</b>	<b>.4880</b>	<b>.4840</b>	<b>.4801</b>	<b>.4761</b>	<b>.4721</b>	<b>.4681</b>	<b>.4641</b>	<b>4</b>	<b>8</b>	<b>12</b>	<b>16</b>	<b>20</b>	<b>24</b>	<b>28</b>	<b>32</b>	<b>36</b>		
<b>0.1</b>	<b>.4602</b>	<b>.4562</b>	<b>.4522</b>	<b>.4483</b>	<b>.4443</b>	<b>.4404</b>	<b>.4364</b>	<b>.4325</b>	<b>.4286</b>	<b>.4247</b>	<b>4</b>	<b>8</b>	<b>12</b>	<b>16</b>	<b>20</b>	<b>24</b>	<b>28</b>	<b>32</b>	<b>36</b>		
<b>0.2</b>	<b>.4207</b>	<b>.4168</b>	<b>.4129</b>	<b>.4090</b>	<b>.4052</b>	<b>.4013</b>	<b>.3974</b>	<b>.3936</b>	<b>.3897</b>	<b>.3859</b>	<b>4</b>	<b>8</b>	<b>12</b>	<b>15</b>	<b>19</b>	<b>23</b>	<b>27</b>	<b>31</b>	<b>35</b>		
<b>0.3</b>	<b>.3821</b>	<b>.3783</b>	<b>.3745</b>	<b>.3707</b>	<b>.3669</b>	<b>.3632</b>	<b>.3594</b>	<b>.3557</b>	<b>.3520</b>	<b>.3483</b>	<b>4</b>	<b>7</b>	<b>11</b>	<b>15</b>	<b>19</b>	<b>22</b>	<b>26</b>	<b>30</b>	<b>34</b>		
<b>0.4</b>	<b>.3446</b>	<b>.3409</b>	<b>.3372</b>	<b>.3336</b>	<b>.3300</b>	<b>.3264</b>	<b>.3228</b>	<b>.3192</b>	<b>.3156</b>	<b>.3121</b>	<b>4</b>	<b>7</b>	<b>11</b>	<b>14</b>	<b>18</b>	<b>22</b>	<b>25</b>	<b>29</b>	<b>32</b>		
<b>0.5</b>	<b>.3085</b>	<b>.3050</b>	<b>.3015</b>	<b>.2981</b>	<b>.2946</b>	<b>.2912</b>	<b>.2877</b>	<b>.2843</b>	<b>.2810</b>	<b>.2776</b>	<b>3</b>	<b>7</b>	<b>10</b>	<b>14</b>	<b>17</b>	<b>20</b>	<b>24</b>	<b>27</b>	<b>31</b>		
<b>0.6</b>	<b>.2743</b>	<b>.2709</b>	<b>.2676</b>	<b>.2643</b>	<b>.2611</b>	<b>.2578</b>	<b>.2546</b>	<b>.2514</b>	<b>.2483</b>	<b>.2451</b>	<b>3</b>	<b>7</b>	<b>10</b>	<b>13</b>	<b>16</b>	<b>19</b>	<b>23</b>	<b>26</b>	<b>29</b>		
<b>0.7</b>	<b>.2420</b>	<b>.2389</b>	<b>.2358</b>	<b>.2327</b>	<b>.2296</b>	<b>.2266</b>	<b>.2236</b>	<b>.2206</b>	<b>.2177</b>	<b>.2148</b>	<b>3</b>	<b>6</b>	<b>9</b>	<b>12</b>	<b>15</b>	<b>18</b>	<b>21</b>	<b>24</b>	<b>27</b>		
<b>0.8</b>	<b>.2119</b>	<b>.2090</b>	<b>.2061</b>	<b>.2033</b>	<b>.2005</b>	<b>.1977</b>	<b>.1949</b>	<b>.1922</b>	<b>.1894</b>	<b>.1867</b>	<b>3</b>	<b>5</b>	<b>8</b>	<b>11</b>	<b>14</b>	<b>16</b>	<b>19</b>	<b>22</b>	<b>25</b>		
<b>0.9</b>	<b>.1841</b>	<b>.1814</b>	<b>.1788</b>	<b>.1762</b>	<b>.1736</b>	<b>.1711</b>	<b>.1685</b>	<b>.1660</b>	<b>.1635</b>	<b>.1611</b>	<b>3</b>	<b>5</b>	<b>8</b>	<b>10</b>	<b>13</b>	<b>15</b>	<b>18</b>	<b>20</b>	<b>23</b>		
<b>1.0</b>	<b>.1587</b>	<b>.1562</b>	<b>.1539</b>	<b>.1515</b>	<b>.1492</b>	<b>.1469</b>	<b>.1446</b>	<b>.1423</b>	<b>.1401</b>	<b>.1379</b>	<b>2</b>	<b>5</b>	<b>7</b>	<b>9</b>	<b>12</b>	<b>14</b>	<b>16</b>	<b>19</b>	<b>21</b>		
<b>1.1</b>	<b>.1357</b>	<b>.1335</b>	<b>.1314</b>	<b>.1292</b>	<b>.1271</b>	<b>.1251</b>	<b>.1230</b>	<b>.1210</b>	<b>.1190</b>	<b>.1170</b>	<b>2</b>	<b>4</b>	<b>6</b>	<b>8</b>	<b>10</b>	<b>12</b>	<b>14</b>	<b>16</b>	<b>18</b>		
<b>1.2</b>	<b>.1151</b>	<b>.1131</b>	<b>.1112</b>	<b>.1093</b>	<b>.1073</b>	<b>.1056</b>	<b>.1038</b>	<b>.1020</b>	<b>.1003</b>	<b>.0985</b>	<b>2</b>	<b>4</b>	<b>6</b>	<b>7</b>	<b>9</b>	<b>11</b>	<b>13</b>	<b>15</b>	<b>17</b>		
<b>1.3</b>	<b>.0968</b>	<b>.0951</b>	<b>.0934</b>	<b>.0918</b>	<b>.0901</b>	<b>.0885</b>	<b>.0869</b>	<b>.0853</b>	<b>.0838</b>	<b>.0823</b>	<b>2</b>	<b>3</b>	<b>5</b>	<b>6</b>	<b>8</b>	<b>10</b>	<b>11</b>	<b>13</b>	<b>14</b>		
<b>1.4</b>	<b>.0808</b>	<b>.0793</b>	<b>.0778</b>	<b>.0764</b>	<b>.0749</b>	<b>.0735</b>	<b>.0721</b>	<b>.0708</b>	<b>.0694</b>	<b>.0681</b>	<b>1</b>	<b>3</b>	<b>4</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>10</b>	<b>11</b>	<b>13</b>		
<b>1.5</b>	<b>.0668</b>	<b>.0655</b>	<b>.0643</b>	<b>.0630</b>	<b>.0618</b>	<b>.0606</b>	<b>.0594</b>	<b>.0582</b>	<b>.0571</b>	<b>.0559</b>	<b>1</b>	<b>2</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>10</b>	<b>11</b>		
<b>1.6</b>	<b>.0548</b>	<b>.0537</b>	<b>.0526</b>	<b>.0516</b>	<b>.0505</b>	<b>.0495</b>	<b>.0485</b>	<b>.0475</b>	<b>.0465</b>	<b>.0455</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>		
<b>1.7</b>	<b>.0446</b>	<b>.0436</b>	<b>.0427</b>	<b>.0418</b>	<b>.0409</b>	<b>.0401</b>	<b>.0392</b>	<b>.0384</b>	<b>.0375</b>	<b>.0367</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>		
<b>1.8</b>	<b>.0359</b>	<b>.0351</b>	<b>.0344</b>	<b>.0336</b>	<b>.0329</b>	<b>.0322</b>	<b>.0314</b>	<b>.0307</b>	<b>.0301</b>	<b>.0294</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>6</b>		
<b>1.9</b>	<b>.0287</b>	<b>.0281</b>	<b>.0274</b>	<b>.0268</b>	<b>.0262</b>	<b>.0256</b>	<b>.0250</b>	<b>.0244</b>	<b>.0239</b>	<b>.0233</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>4</b>	<b>5</b>	<b>5</b>		
<b>2.0</b>	<b>.0228</b>	<b>.0222</b>	<b>.0217</b>	<b>.0212</b>	<b>.0207</b>	<b>.0202</b>	<b>.0197</b>	<b>.0192</b>	<b>.0188</b>	<b>.0183</b>	<b>0</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>3</b>	<b>3</b>	<b>4</b>	<b>4</b>		
<b>2.1</b>	<b>.0179</b>	<b>.0174</b>	<b>.0170</b>	<b>.0166</b>	<b>.0162</b>	<b>.0158</b>	<b>.0154</b>	<b>.0150</b>	<b>.0146</b>	<b>.0143</b>	<b>0</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>3</b>	<b>3</b>	<b>4</b>		
<b>2.2</b>	<b>.0139</b>	<b>.0136</b>	<b>.0132</b>	<b>.0129</b>	<b>.0125</b>	<b>.0122</b>	<b>.0119</b>	<b>.0116</b>	<b>.0113</b>	<b>.0110</b>	<b>0</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>3</b>	<b>3</b>		
<b>2.3</b>	<b>.0107</b>	<b>.0104</b>	<b>.0102</b>		<b>.0990</b>	<b>.0964</b>	<b>.0939</b>	<b>.0914</b>			<b>0</b>	<b>2</b>	<b>8</b>	<b>10</b>	<b>13</b>	<b>15</b>	<b>18</b>	<b>20</b>	<b>23</b>		
											<b>3</b>	<b>5</b>	<b>8</b>	<b>10</b>	<b>13</b>	<b>15</b>	<b>18</b>	<b>20</b>	<b>23</b>		
<b>2.4</b>	<b>.0^820</b>	<b>.0^798</b>	<b>.0^776</b>	<b>.0^755</b>	<b>.0^734</b>		<b>.0^714</b>	<b>.0^695</b>	<b>.0^676</b>	<b>.0^657</b>	<b>.0^639</b>	<b>2</b>	<b>4</b>	<b>6</b>	<b>7</b>	<b>9</b>	<b>11</b>	<b>13</b>	<b>15</b>	<b>17</b>	
							<b>.0^714</b>	<b>.0^695</b>	<b>.0^676</b>	<b>.0^657</b>	<b>.0^639</b>	<b>2</b>	<b>4</b>	<b>6</b>	<b>7</b>	<b>9</b>	<b>12</b>	<b>14</b>	<b>16</b>	<b>18</b>	
<b>2.5</b>	<b>.0^621</b>	<b>.0^604</b>	<b>.0^587</b>	<b>.0^570</b>	<b>.0^554</b>	<b>.0^539</b>	<b>.0^523</b>	<b>.0^508</b>	<b>.0^494</b>	<b>.0^480</b>	<b>2</b>	<b>3</b>	<b>5</b>	<b>6</b>	<b>8</b>	<b>9</b>	<b>11</b>	<b>12</b>	<b>14</b>		
<b>2.6</b>	<b>.0^466</b>	<b>.0^453</b>	<b>.0^440</b>	<b>.0^427</b>	<b>.0^415</b>	<b>.0^402</b>	<b>.0^391</b>	<b>.0^379</b>	<b>.0^368</b>	<b>.0^357</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>10</b>		
<b>2.7</b>	<b>.0^347</b>	<b>.0^336</b>	<b>.0^326</b>	<b>.0^317</b>	<b>.0^307</b>	<b>.0^298</b>	<b>.0^289</b>	<b>.0^280</b>	<b>.0^272</b>	<b>.0^264</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>		
<b>2.8</b>	<b>.0^256</b>	<b>.0^248</b>	<b>.0^240</b>	<b>.0^233</b>	<b>.0^226</b>	<b>.0^219</b>	<b>.0^212</b>	<b>.0^205</b>	<b>.0^199</b>	<b>.0^193</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>6</b>		
<b>2.9</b>	<b>.0^187</b>	<b>.0^181</b>	<b>.0^175</b>	<b>.0^169</b>	<b>.0^164</b>	<b>.0^159</b>	<b>.0^154</b>	<b>.0^149</b>	<b>.0^144</b>	<b>.0^139</b>	<b>0</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>3</b>	<b>3</b>	<b>4</b>	<b>4</b>		
<b>3.0</b>	<b>.0^135</b>	<b>.0^131</b>	<b>.0^126</b>	<b>.0^122</b>	<b>.0^118</b>	<b>.0^114</b>	<b>.0^111</b>	<b>.0^107</b>	<b>.0^104</b>	<b>.0^100</b>	<b>0</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>3</b>	<b>3</b>	<b>4</b>		

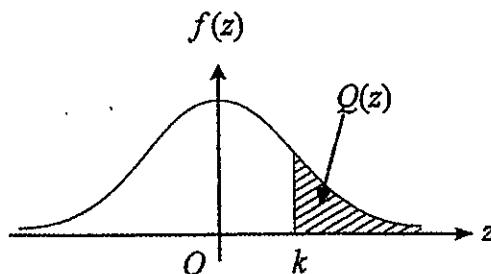
For negative  $z$  use relation:

*Bagi z negatif guna hubungan:*

$$Q(z) = 1 - Q(-z) = P(-z)$$

$$f(z) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2}z^2\right)$$

$$Q(z) = \int_k^{\infty} f(z) dz$$



#### **Example / Contoh:**

If  $X \sim N(0, 1)$ , then

Jika  $X \sim N(0, 1)$ , maka

$$P(X \geq k) = O(k)$$

$$P(X > 2.1) = Q(2.1) = 0.0$$

[Lihat halaman sebelah

**MAKLUMAT UNTUK CALON**

1. Kertas soalan ini mengandungi dua bahagian : **Bahagian A dan Bahagian B.**  
*This question paper consists of two sections: Section A and Section B.*
2. Jawab semua soalan dalam **Bahagian A** dan mana-mana **dua** soalan daripada **Bahagian B.**  
*Answer all questions in Section A and any two questions from Section B.*
3. Jawapan anda hendaklah ditulis dalam ruangan yang disediakan dalam kertas peperiksaan. Sekiranya ruangan tidak mencukupi, sila dapatkan helaian tambahan daripada pengawas peperiksaan.  
*Write your answer on the spaces provided in the question paper. If the spaces is insufficient, you may ask for 'helaian tambahan' from the invigilator.*
4. Tunjukkan langkah-langkah penting dalam kerja mengira anda. Ini boleh membantu anda untuk mendapat markah.  
*Show your working. It may help you to get marks.*
5. Rajah yang mengiringi soalan tidak dilukis mengikut skala kecuali dinyatakan.  
*The diagrams in the questions provided are not drawn to scale unless stated.*
6. Markah yang diperuntukkan bagi setiap soalan dan ceraian soalan ditunjukkan dalam kurungan.  
*The marks allocated for each question and sub-part of the question are shown in brackets.*
7. Jadual Kebarangkalian Hujung Atas  $Q(z)$  Bagi Taburan Normal  $N(0,1)$  disediakan di halaman 35.  
*The Upper Tail Probability  $Q(z)$  For The Normal Distribution  $N(0,1)$  Table is provided on page 35.*
8. Satu senarai rumus disediakan di halaman 2 dan 3.  
*A list of formulae is provided on page 2 and 3.*
9. Anda dibenarkan menggunakan kalkulator saintifik yang tidak boleh diprogramkan.  
*You may use a non-programmable scientific calculator.*
10. Ikat helaian tambahan bersama-sama dengan 'buku soalan' dan serahkan kepada pengawas peperiksaan pada akhir peperiksaan.  
*Tie the 'helaian tambahan' together with the 'buku soalan' and hand in to the invigilator at the end of the examination.*