

**MODUL PERKEMBANGAN PEMBELAJARAN
PEPERIKSAAN PERCUBAAN SPM 2024**

MATEMATIK TAMBAHAN

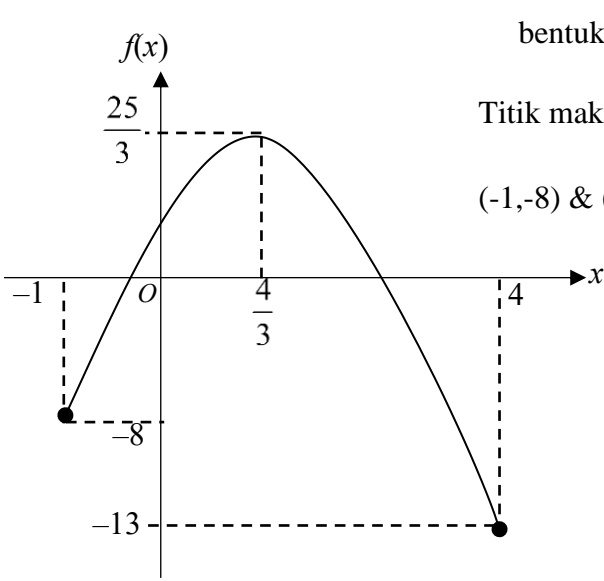
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Kertas 2

PERATURAN PEMARKAHAN

**PERATURAN PERMARKAHAN MATEMATIK TAMBAHAN KERTAS 2
PEPERIKSAAN PERCUBAAN SPM 2024**

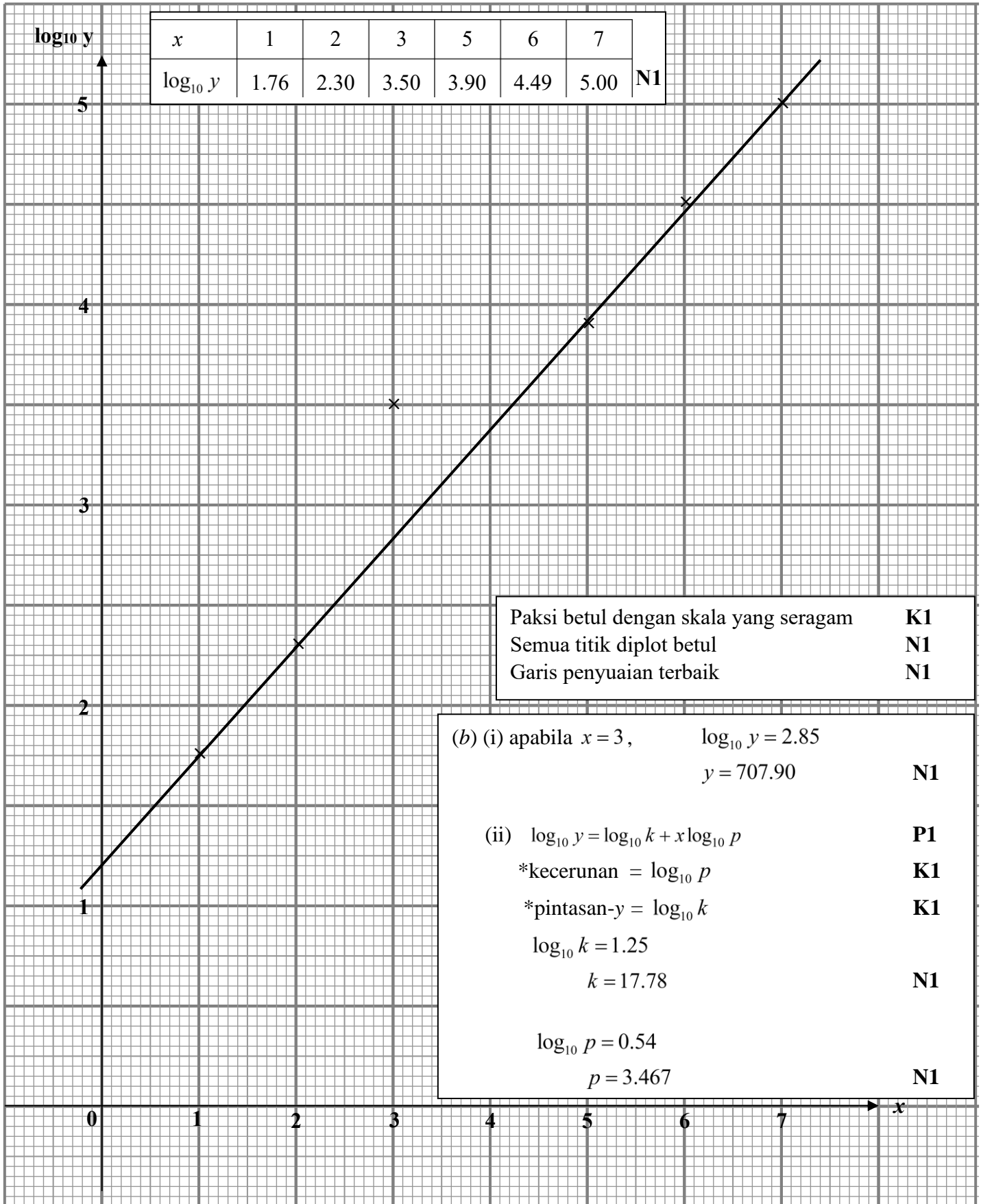
No	Peraturan Pemarkahan	Jumlah
1	<p>(a) $\angle KOL = 60^\circ \times \frac{\pi}{180^\circ}$ $\frac{1}{3}\pi$</p> <p>(b) $\frac{1}{2}(12\sqrt{3})^2 \left(\frac{1}{3}\pi\right)$ $\frac{1}{2}(12\sqrt{3})(12\sqrt{3})\sin^*(60^\circ)$ $\frac{1}{2}(12\sqrt{3})^2 \left(\frac{1}{3}\pi\right) - \frac{1}{2}(12\sqrt{3})(12\sqrt{3})\sin^*(60^\circ)$ 39.16 (terima : $72\pi - 108\sqrt{3}$)</p>	<p>K1</p> <p>N1</p> <p>K1</p> <p>K1</p> <p>K1</p> <p>N1</p> <p>6</p>
2	<p>(a) $0.123 + 0.000123 + 0.000000123 + \dots$ $\frac{0.123}{1 - 0.001}$ $h = 41$</p> <p>(b) (i) $3\pi, 4.5\pi, 6.75\pi$ (ii) $T_5 = 6(1.5^{5-1})$ 30.375 (iii) $62.34375\pi = \frac{3\pi(1.5^n - 1)}{1.5 - 1}$ $n = 6$</p>	<p>P1</p> <p>K1</p> <p>N1</p> <p>P1</p> <p>K1</p> <p>N1</p> <p>K1</p> <p>N1</p> <p>8</p>

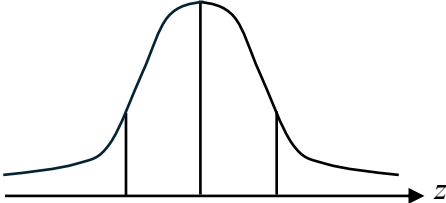
3	<p>(a) $f(x) = -3 \left(x^2 - \frac{8}{3}x + \left(\frac{-8}{2} \right)^2 - \left(\frac{-8}{2} \right)^2 \right) + 3$ K1</p> <p>$f(x) = -3 \left(x - \frac{4}{3} \right)^2 + \frac{25}{3}$ N1</p> <p>Nilai maksimum dan $\frac{25}{3} // 8\frac{1}{3} // 8.333$ N1</p> <p>(b)  bentuk \wedge P1 Titik maksimum $\left(\frac{4}{3}, \frac{25}{3} \right)$ dan $(-1, -8) \ \& \ (4, -13)$ P1</p> <p>$-\frac{25}{3} \leq f(x) \leq 13$ N1</p>	6
4	<p>(a) $\frac{y - (-1)}{x - 6} \times \frac{y - (-9)}{x - 4} = -1$ K1</p> <p>$x^2 + y^2 - 10x + 10y + 33 = 0$ N1</p> <p>(b) $(-4y - 15)^2 + y^2 - 10(-4y - 15) + 10y + 33 = 0$ K1</p> <p>$(y + 6)(y + 4) = 0$ K1</p> <p>$y = -6$, $y = -4$</p> <p>$x = 9$, $x = 1$</p> <p>$R(9, -6)$ N1</p> <p>$T(1, -4)$ N1</p>	6

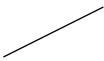

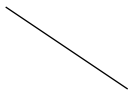
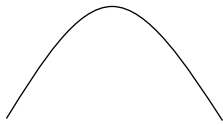
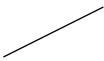

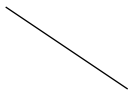
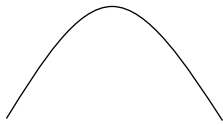
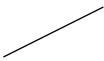

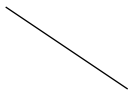
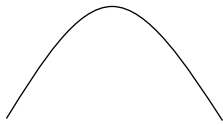
5	<p>(a) (i) $a = 2, b = \frac{3}{2}$ N1N1</p> <p>(ii) 2 N1</p> <p>Nota : N0 jika pengiraan $y = 2$ <i>tidak</i> ditunjukkan.</p> <p>(b) (i) Guna $\cos 2x = 2\cos^2 x - 1$ K1 $2\sin x \cos x$ $\sin 2x$ N1</p> <p>(ii) $\cos x(2\sin x + 1) = 0$ P1 $x = 90^\circ, 270^\circ$ or $x = 210^\circ, 330^\circ$ K1 $x = 90^\circ, 210^\circ, 270^\circ, 330^\circ$ N1</p>	8
6	<p>(a) (i) $\left[\frac{4x^{-1}}{(-1)}\right]_2^k = 4\left[\frac{4x^{-1}}{(-1)}\right]_k^8$ K1</p> <p>$\left[\left(-\frac{4}{k}\right) - \left(-\frac{4}{2}\right)\right] = 4\left[\left(-\frac{4}{8}\right) - \left(-\frac{4}{k}\right)\right]$ K1</p> <p>$k = 5$ N1</p> <p>(ii) $\left(-\frac{4}{8}\right) - \left(-\frac{4}{5^*}\right)$ K1</p> <p>$\frac{3}{10}$ N1</p> <p>(b) $\pi\left[-\frac{16}{3x^3}\right]_2^8$ K1</p> <p>$\pi\left[\left(-\frac{16}{3(8)^3}\right) - \left(-\frac{16}{3(2)^3}\right)\right]$ K1</p> <p>$\frac{21}{32}\pi$ N1</p>	8

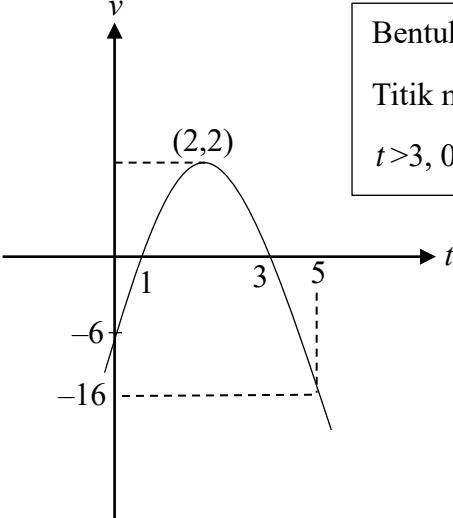
7	<p>(a) $x = 2y + 1$</p> <p>$2(2y + 1)^2 + y^2 - 2(2y + 1) - 3y = 17$</p> $y = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(9)(-17)}}{2(9)}$ <p>$y = 1.320, -1.431$</p> <p>$x = 3.640, -1.862$</p> <p>(b) $5 + a^2 - 14 = 0$</p> <p>$a - 3 = 0$</p> <p>$a = 3$</p>	<p>P1</p> <p>K1</p> <p>K1</p> <p>N1</p> <p>N1</p> <p>P1</p> <p>P1</p> <p>N1</p>	<p>8</p>
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No. 8



9	<p>(a) ${}^{10}C_8(0.85)^8(0.15)^2 @ {}^{10}C_9(0.85)^9(0.15)^1 @ {}^{10}C_{10}(0.85)^{10}(0.15)^0$ K1</p> <p>${}^{10}C_8(0.85)^8(0.15)^2 + {}^{10}C_9(0.85)^9(0.15)^1 + {}^{10}C_{10}(0.85)^{10}(0.15)^0$ K1</p> <p>0.8202 N1</p> <p>(b)(i) $P\left(Z < \frac{18.5 - 22.5}{3.2}\right)$ P1</p> <p>0.1056 N1</p> <p>(ii)</p> <p>Lakar</p>  <p>Nota :</p> <ul style="list-style-type: none"> - Mempunyai 3 rantau - Paksi z dilabel - Garis lurus menggunakan alat tepi lurus <p>$P\left(\frac{18.5 - 22.5}{3.2} \leq Z < \frac{m - 22.5}{3.2}\right)$ P1</p> <p>$z = 0.781$ P1</p> <p>$\frac{m - 22.5}{3.2} = 0.781$ K1</p> <p>25 N1</p>	10
10	<p>(a) (i) $\vec{ST} = \vec{SR} + \vec{RT}$ K1</p> <p>$= -6\vec{m} + 18\vec{n}$ N1</p> <p>(ii) $\vec{RV} = \frac{3}{2}\vec{m} + \frac{27}{2}\vec{n}$ N1</p> <p>(b) $d\left(\frac{3}{2}\vec{m} + \frac{27}{2}\vec{n}\right) = 18\vec{n} + e(2\vec{m} - 7\vec{n})$ K1</p> <p>$\frac{27}{2}d = 18 - 7e$ atau $\frac{3}{2}d = 2e$ K1</p> <p>$e = \frac{18}{25}, d = \frac{24}{25}$ N1, N1</p>	10

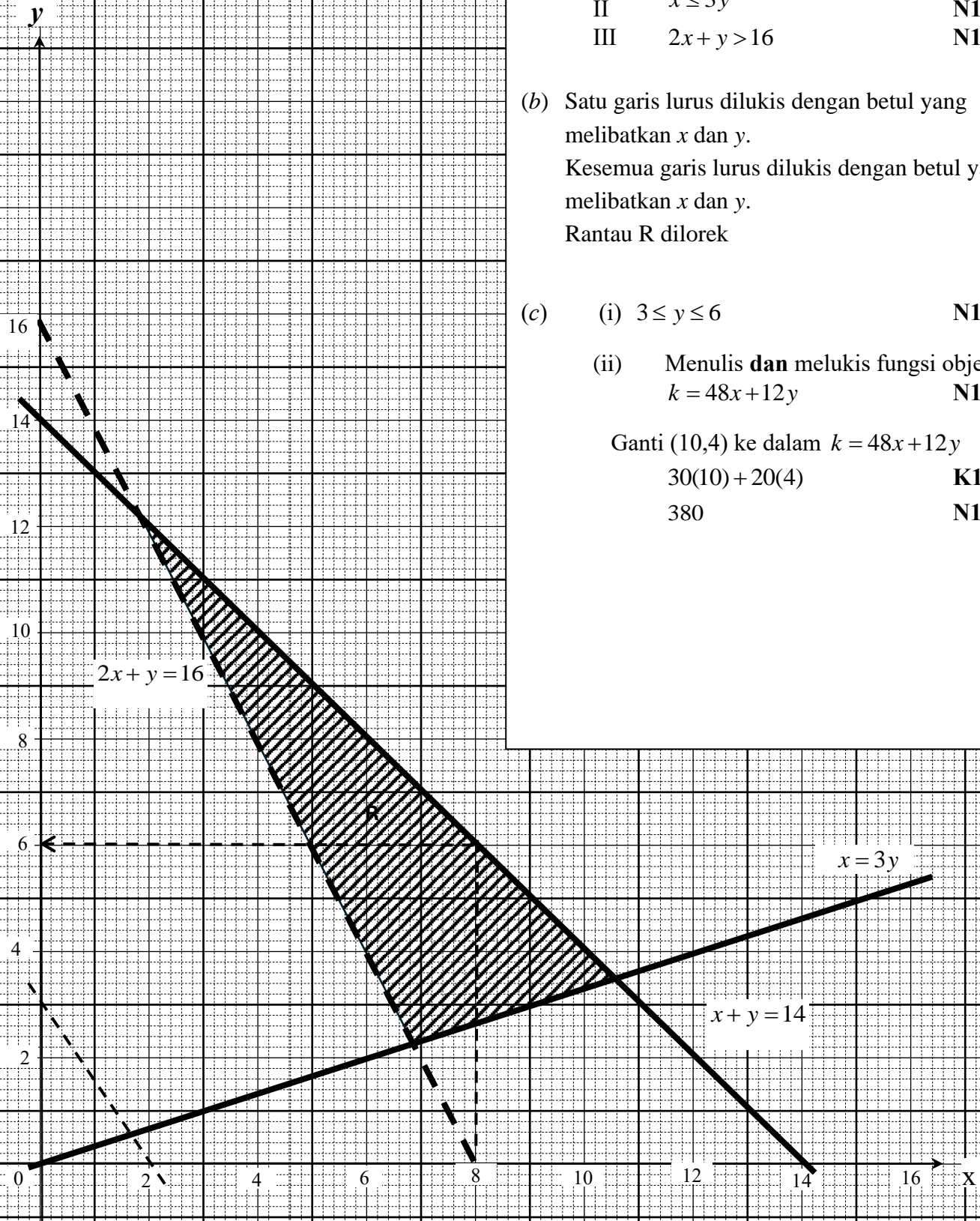
	<p>(c) $\overrightarrow{RW} = \lambda \overrightarrow{RV}$</p> $gm + 2n = \lambda \left(\frac{3}{2}m + \frac{27}{2}n \right)$ $\frac{3}{2}\lambda = g \text{ atau } \frac{27}{2}\lambda = 2$ $g = \frac{2}{9}$	<p>K1</p> <p>K1</p> <p>N1</p>																					
11	<p>(a) 4</p> <p>(b) guna $\frac{dy}{dx}$ dan ganti $x = 5$</p> $-2(5) + 4$ -6 <p>(c) $m \times (-6) = -1$</p> $y - 7 = \left(\frac{1}{6} \right) (x - 5) \text{ @ setara}$ $y = \frac{1}{6}x + \frac{37}{6}$ <p>(d) guna $\frac{dy}{dx} = 0$ dan selesaikan</p> $-2x + 4 = 0$ <p>(2, 16)</p> <p>Bina jadual</p> <table border="1" style="width: 100%; text-align: center;"> <tbody> <tr> <td>x</td> <td>1.5</td> <td>2</td> <td>2.5</td> </tr> <tr> <td>$\frac{dy}{dx}$</td> <td>1</td> <td>0</td> <td>-1</td> </tr> <tr> <td>Tanda bagi $\frac{dy}{dx}$</td> <td>+</td> <td>0</td> <td>-</td> </tr> <tr> <td>Lakaran tangen</td> <td></td> <td></td> <td></td> </tr> <tr> <td>Lakaran graf</td> <td colspan="3"></td> </tr> </tbody> </table> <p>titik maksimum</p>	x	1.5	2	2.5	$\frac{dy}{dx}$	1	0	-1	Tanda bagi $\frac{dy}{dx}$	+	0	-	Lakaran tangen				Lakaran graf				<p>N1</p> <p>K1</p> <p>N1</p> <p>K1</p> <p>K1</p> <p>N1</p> <p>K1</p> <p>N1</p> <p>K1</p> <p>N1</p> <p>K1</p> <p>N1</p>	10
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Tanda bagi $\frac{dy}{dx}$	+	0	-																				
Lakaran tangen																							
Lakaran graf																							

12	<p>(a) (i) $-6 = -m(0-2)^2 + 2$ K1</p> <p style="text-align: center;">$m = 2$ N1</p> <p>(ii) $0 = -2(t-2)^2 + 2$ dan selesaikan persamaan kuadratik K1</p> <p style="text-align: center;">$t = 1, t = 3$ N1</p> <p>(b)</p> <div style="display: flex; align-items: center;">  <table border="1" style="margin-left: 20px;"> <tbody> <tr> <td>Bentuk graf</td> <td>P1</td> </tr> <tr> <td>Titik max (2,2), (0,-6) dan (5,-16)</td> <td>N1</td> </tr> <tr> <td>$t > 3, 0 < t < 1$</td> <td>N1</td> </tr> </tbody> </table> </div> <p>(c) $\int_2^3 -2t^2 + 8t - 6dt @ \left \int_3^5 -2t^2 + 8t - 6dt \right$ kamir dan penggantian K1</p> <p>$\int_2^3 -2t^2 + 8t - 6dt + \left \int_3^5 -2t^2 + 8t - 6dt \right$ penambahan K1</p> <p style="text-align: center;">$\frac{44}{3}$ N1</p>	Bentuk graf	P1	Titik max (2,2), (0,-6) dan (5,-16)	N1	$t > 3, 0 < t < 1$	N1	
Bentuk graf	P1							
Titik max (2,2), (0,-6) dan (5,-16)	N1							
$t > 3, 0 < t < 1$	N1							
13	<p>(a) $\frac{\sin T}{70} = \frac{\sin 50.69}{90}$ K1</p> <p style="text-align: center;">$T = 37^\circ$ N1</p> <p style="text-align: center;">$TN^2 = 90^2 + 70^2 - 2(90)(70)\cos 92.31^\circ$ K1</p> <p style="text-align: center;">$TN = 116.22$ N1</p> <p>(b) $\cos 37^\circ = \frac{TN}{90}$ K1</p> <p style="text-align: center;">71.88 N1</p>							

	(c) $\sin 50.69 = \frac{MA}{70} @ \sqrt{70^2 - 44.34^2}$	K1	
	$MA = 54.16 / 54.15$	N1	
	$s = \frac{54.16 + 70 + 44.34}{2}$ dan		
	$L = \sqrt{84.25^* (84.25 - 54.16^*) (84.25 - 70) (84.25 - 44.34)}$ ATAU setara	K1	
	$L = 1200.73$	N1	

No. 14

- (a) I $x + y \leq 14$ N1
II $x \leq 3y$ N1
III $2x + y > 16$ N1
- (b) Satu garis lurus dilukis dengan betul yang melibatkan x dan y . K1
Kesemua garis lurus dilukis dengan betul yang melibatkan x dan y . K1
Rantau R dilorek N1
- (c) (i) $3 \leq y \leq 6$ N1
(ii) Menulis **dan** melukis fungsi objektif $k = 48x + 12y$ N1
Ganti $(10, 4)$ ke dalam $k = 48x + 12y$
 $30(10) + 20(4)$ K1
 380 N1



15	<p>(a) $p = \frac{9}{8} \times 100 @ \frac{q}{3} \times 100 = 105 @ \frac{4.80}{r} \times 100 = 120$</p> <p>$p = 112.50, q = 3.15, r = 4.00$ (semua betul)</p> <p>Nota : 2 betul (N1)</p> <p>(b) $\frac{(112.5 \times 20) + (105 \times 30) + (108 \times 10) + (120 \times 40)}{20 + 30 + 10 + 40}$</p> <p>112.80</p> <p>(c) $\frac{C_{23}}{43} \times 100 = 112.8$</p> <p>48.50</p> <p>(d) $\frac{112.8 \times 110}{100}$</p> <p>124.08</p>	<p>K1</p> <p>N1N1</p> <p>K1 K1</p> <p>N1</p> <p>K1</p> <p>N1</p> <p>K1</p> <p>N1</p>	<p>10</p>
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PERATURAN PEMARKAHAN TAMAT